



# Performance Analysis of OFDM system using LS, MMSE and Less Complex MMSE in terms of BER, SNR and MSE

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**Abstract:** *In this research, Channel estimation has been accomplished for OFDM framework. In wireless communication, because of a nonappearance of channel estimation a decent execution of communication doesn't accomplish. Also, it is critical for wireless communication that transmission of information at high rate and transmission with least mistake could conceivable. Such a variety of times in remote correspondence, abundance of a sign get vacillated. This variance influences the execution of wireless communication. So to beat these issues channel estimation is essential. In channel estimation pilots get joined with transmitting information, and this consolidated data goes through channel and reaches at recipient. At accepting side estimation get perform with the assistance of those pilots. OFDM have a significance in remote correspondence as OFDM gives high rate of data, additionally it gives low multipath contortion, these properties are essential to increase great execution of remote correspondence. This is motivation to choose OFDM in this study. This concentrate essentially thinks about three distinct calculations for divert estimation in OFDM framework. Likewise this study contrasts these calculations and traditional OFDM. This study utilizes comb type pilot insertion method, and this procedure is extremely valuable to diminish the impact of fast fading in wireless communication environment.*

## I. INTRODUCTION

Wireless systems are relied upon to require high information rates with low postpone and low bit error rate (BER). In such circumstances, the execution of wireless communication is mostly represented by the remote channel environment. What's more, high information rate transmission and high portability of transmitters and/or collectors more often than not bring about frequency selective and time-specific, i.e., doubly particular, fading channels for future versatile broadband remote frameworks. In this way, moderating such doubly particular fading impacts is basic for effective information transmission. Additionally, idealize channel state information (CSI) is not accessible at the collector. Consequently by and by, precise appraisal of the CSI majorly affects the entire framework execution [1]. It is likewise on the grounds that, as opposed to the ordinarily static and unsurprising attributes of a wired channel, the remote channel is somewhat alert and erratic, which makes an accurate examination of the remote correspondence framework frequently troublesome. For a commonplace wireless system, RF signal transmission between two radio wires usually experiences power misfortune, which influences its execution. This force misfortune amongst transmitter and recipient is a consequence of three unique marvels: 1) separation subordinate lessening of the influence thickness called way misfortune or free space constriction, 2) ingestion because of the particles in the climate and 3) signal blurring brought on by landscape and climate conditions in the proliferation way. Climatic assimilation is because of the electrons, uncondensed water vapor and atoms of different gasses. Way misfortune is a hypothetical constriction which happens under free viewable pathway conditions and which increments with the separation between base station and versatile. Fading alludes to the variety of the sign adequacy after some time and frequency. Conversely with the added substance commotion as the most widely recognized wellspring of sign debasement, fading is another wellspring of sign corruption that is portrayed as a non-added substance signal aggravation in the wireless channel. Blurring might be either because of multipath propagation, alluded to as multi-way (impelled) fading, or to shadowing from deterrents that influence the spread of a radio wave, alluded to as shadow fading. Fading channel models are frequently used to show electromagnetic transmission of data over remote media, for example, phone and telecast correspondence.

Rayleigh fading is a consequence of a gathering of a few signs at the recipient approaching and reflected from a wide range of articles and bearings in the zone. Because of their distinctive voyaging separations, the signs are typically not in stage, strengthening or quenching each other. The development of the terminal causes consistent and flighty varieties of the sign stages after some time, making the constriction fluctuate variable and to a great degree high at some focuses (fading dips). Rayleigh fading is most detectable in urban regions. Plunges will happen all the more much of the time at higher frequencies and faster versatile development. To stay away from plunges it is important to accomplish an adequate blurring edge. The normal estimation of the sign must be in any event the same number of decibels over the beneficiary affectability level as the most grounded expected plunge. To beat these issues uncommon gathering procedures are typically utilized, specifically the different recipient joining systems known as diversity [2].



Large scale fading happens as the versatile travels through a vast separation, for instance, a separation of the request of cell size. It is brought about by way loss of sign as a component of separation and shadowing by substantial protests, for example, structures, mediating territories, and vegetation. Shadowing is a moderate blurring process portrayed by variety of middle way misfortune between the transmitter and collector in altered areas. At the end of the day, large scale fading is described by normal way misfortune and shadowing. Then again, small scale fading alludes to fast variety of sign levels because of the valuable and damaging impedance of different sign ways (multi-ways) when the versatile station moves short separations. Contingent upon the relative degree of a multipath, recurrence selectivity of a channel is portrayed (e.g., by frequency particular or frequency level) for little scaling blurring. In the interim, contingent upon the time variety in a channel because of versatile rate (portrayed by the Doppler spread), short term fading can be delegated either fast fading or moderate blurring. This paper concentrates on examining the impact of fading in digital communication methods, for example, orthogonal frequency division multiplexing (OFDM). It is on the grounds that OFDM is most generally utilized as a part of in modern mobile broadband wireless communication frameworks, for example, portable WiMAX and long-term evolution (LTE). Hence, channel estimation procedures for OFDM frameworks in doubly specific channels are the point of enthusiasm for this paper. Because of its high data transfer capacity productivity, its basic execution and its strength over frequency particular channels, OFDM has been generally connected in wireless communication frameworks. For traditional reasonable discovery, exact CSI is required for the recipient handling. Despite the fact that channel estimation can be dodged by utilizing differential balance procedures, these strategies will fizzle calamitously in the fast fading channel, where the channel impulse response (CIR) fluctuates essentially inside the image length. Indeed, differential tweak systems accept that the channel is stationary over the time of two OFDM images which is not valid for the quick blurring channels. The orthogonality among the subcarriers is wrecked and inter carrier interferences (ICI) is made, which, if left uncompensated can bring about high bit error rates (BERs). By and large, the pay for the ICI because of the fast fading channel depends on more mind boggling equalizers, for example, minimum mean-square error (MMSE) equalizers, which need the individual subcarrier recurrence reactions as well as the obstruction among subcarriers in each OFDM image. Subsequently, channel estimation is all the more trying for OFDM frameworks in fast fading diverts than in moderate blurring frameworks. As such, the channel estimation is a basic part of the collector for fast fading channels and the beneficiary needs to perform channel estimation for each OFDM image. Mixed media remote administrations require high information rate transmission over portable radio channels. Orthogonal Frequency Division Multiplexing (OFDM) is generally considered as a promising decision for future remote interchanges frameworks because of its high-information rate transmission ability with high data transfer capacity productivity. In OFDM, the whole channel is isolated into numerous thin sub-channels, changing over a frequency particular channel into a gathering of frequency flat channels. In addition, inter-symbol interference (ISI) is evaded by the utilization of cyclic prefix (CP), which is accomplished by augmenting an OFDM image with some segment of its head or tail [3]. Truth be told, OFDM has been received in digital audio broadcasting (DAB), digital video broadcasting (DVB), and digital subscriber line (DSL), and wireless local area network (WLAN) principles, for example, the IEEE 802.11a/b/g/n [4]. It has additionally been received for remote broadband access norms, for example, the IEEE 802.16e, and as the center procedure for the fourth-generation (4G) wireless mobile Communications [5]. To kill the requirement for channel estimation and following, quadrature phase shift keying (QPSK) can be utilized as a part of OFDM frameworks [6]. The execution of OFDM frameworks can be enhanced by taking into consideration cognizant demodulation when an exact channel estimation procedure is used [7].

This paper is sorted out in taking after area: Section II depicts a procedure of channel estimation, in which two distinctive sorts of pilot estimation methods has been portrayed. Segment III spreads essential idea of OFDM framework with three distinctive channel estimation calculations. At long last simulation results are given in segment IV in which BER, SNR and MSE are the criteria of execution. Finally conclusion has been portrayed in area V.

## II. CHANNEL ESTIMATION

Channel estimation strategies for OFDM frameworks can be gathered into two classifications: blind and non blind. The visually impaired channel estimation technique misuses the factual conduct of the got signals, while the non-blind channel estimation strategy uses a few or all segments of the transmitted signals, i.e., pilot tones or preparing groupings, which are accessible to the recipient to be utilized for the channel estimation.

### BLOCK TYPE

For this situation pilots are embedded in a thick manner in a couple picked images (commonly the introduction image in many principles) with the accompanying images running without pilot. The pilot-thick images are required to yield amazing channel gauges which are then, regularly bolstered into a channel tracker, which yields gauges on the pilot-less images. This worldview is regularly termed semi-blind strategy for channel estimation.

Obviously, the transient dividing it between two continuous pilot-rich images is restricted by the Doppler spread of the earth. Subsequently, this kind of pilot arrangement regularly found in static and low-Doppler situations, for example, wire-line transmissions or altered wireless correspondence frameworks [1].

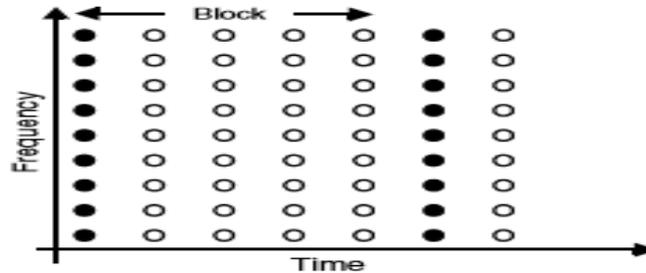


Figure 2.1 shows the basic principle of pilot arrangement in block type.

### COMB TYPE

As opposed to the piece sort case, particular sub-bearers are picked over which pilots are embedded in each image. This takes into account straightforward 1-D (frequency space) addition of the channel at the non-pilot areas and is suited for vehicular and high-Doppler situations. The frequency separating of pilot's  $Df$  in this case restrains the most extreme postponement spread of the channel. Basically, see that an OFDM edge is peppered with pilots in an example which accomplishes a flawless exchange off between estimation precision, Doppler vigor and pilot-overhead. Plans, for example, jumping pilots have been recommended to adventure most extreme frequency diversity [2].

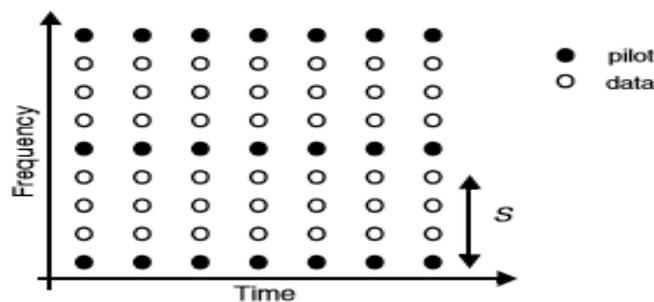


Figure 2.2 shows the basic principle of pilot arrangement in Comb type.

### III. OFDM SYSTEMS

The key components of OFDM frameworks are depicted underneath.

**ORTHOGONALITY:** In OFDM frameworks, the two occasional signals are orthogonal when the integral of their product over a period is equivalent to zero.

**SUB-CARRIERS IN OFDM SYSTEMS:** Each subcarrier in an OFDM framework is a sinusoid with a frequency that is a whole number numerous of crucial frequency. Each subcarrier can be communicated as a Fourier arrangement segment of the composite signal, i.e. an OFDM image.

**INTER SYMBOL INTERFERENCE:** Inter Symbol Interference (ISI) is a type of bending of a signal in which one image meddles with resulting images. This is an undesirable wonder as the past images have comparative impact as commotion; subsequently, making the correspondence less dependable. ISI is typically created by multipath spread or the inalienable non-linear frequency reaction of a channel bringing on progressive images to "obscure" together.



The nearness of ISI in the framework presents mistake in choice gadget at the collector yield. Hence, in the configuration of transmitting and accepting channels, the goal is to minimize the impacts of ISI and; along these lines, convey the computerized information to its destination with the littlest error rate conceivable.

**INTER-CARRIER INTERFERENCE:** Nearness of Doppler movements and frequency and phase offset in an OFDM framework causes misfortune in orthogonality of the subcarriers. Accordingly, obstruction is seen between subcarriers. This marvel is known as inter-carrier interference (ICI). [8]

**CYCLIC PREFIX:** The Cyclic Prefix (CP) or Guard Interval is an intermittent augmentation of the last part of an OFDM image that is added to the front of image in a transmitter, and is evacuated at the beneficiary before demodulation. Cyclic prefix goes about as a guard interim. It wipes out the between image obstruction from the past image [9]. It goes about as a redundancy of the end of the image, in this way permitting the straight convolution of a frequency-selective multipath channel to be displayed as roundabout convolution which thus might be changed to the frequency area utilizing a discrete Fourier change. This methodology takes into consideration basic frequency-domain handling, for example, channel estimation and equalization [10].

**INVERSE DISCRETE FOURIER TRANSFORM:** In frequency space in OFDM, the regulated information images are encouraged onto the orthogonal sub-transporters. Be that as it may, exchange of sign over a divert is just conceivable in now is the ideal time space. Subsequently, IDFT of sign is generally taken some time recently, which changes over the OFDM signal from frequency space to time area. IDFT being a straight change can be effectively connected to the framework and DFT can be connected at the collector end to recover the first information in frequency area at the beneficiary end. As, the premise of Fourier change is orthogonal in nature, the time area likeness OFDM sign can be actualized from its frequency components.[8]

**MODULATION:** In an OFDM framework, the high information rate data is isolated into little bundles of information which are set orthogonal to each other. This is accomplished by tweaking the information by a regulation procedure, for example, QPSK. After this, IFFT is performed on the adjusted sign which is further prepared by going through a parallel-to-serial converter.[9] so as to maintain a strategic distance from ISI, a cyclic prefix is added to the sign as examined previously.

**DEMODULATION:** For this situation, they got information is initially gone through a low pass channel to expel the cyclic prefix. After this, FFT is performed and the serial information acquired is changed over into the parallel signal [11]. A demodulator is utilized to get back the first flag.

**COMMUNICATION CHANNEL:** This is the medium/channel through which the data is transferred. Presence of noise in this medium affects the signal and causes distortion in its data content. [10]

**CHANNEL ESTIMATION ALGORITHM:**

*Channel Estimation using LS Algorithm*

Guard interval is utilized to anticipate ICI. Received signal is communicated after expulsion of ICI as:

$$Y = XH + W$$

In above condition Y is characterizing as got signal vector, and X is characterizing as transmitted signal in a type of diagonal matrix. Presently OFDM signal with least square (LS) estimator is given as:

$$H_{LS} = (X^H X)^{-1} X^H Y$$

Here X is an diagonal matrix, which can diminish estimation.

$$H_{LS} = X^{-1}Y$$

Above condition characterizes an operation of LS estimation. It is essentially accomplished by taking proportion of two received signal to transmitted sign. Where X is characterize as a received signal and Y is characterized as a transmitted signal.

Channel estimation can be characterized at pilot subcarrier as:

$$H_p(m) = Y_p(m) / X_p(m)$$

Channel Estimation Using Linear Interpolation Method

In a nearness of fast fading to get a precise reaction of a channel is extremely troublesome. Since for the most part, reaction of a channel get change after each OFDM image. Utilization of comb type pilot arrangement is exceptionally helpful here. Be that as it may, in a comb type pilot arrangement pilots are connected with all symbols however with some subcarriers. So Interpolation method is critical to characterize the frequency reaction of those subcarriers in which pilots are not appended. In this paper linear interpolation is utilized. It is characterize as:

$$\begin{aligned} H(n) &= H_d(n) \\ &= H_d(mL + l) \\ &= (H_p(m+1) - H_p(m)) \frac{l}{L} + H_p(m) \end{aligned}$$

This equation defines channel estimation at data carrier k.

CHANNEL ESTIMATION USING MINIMUM MEAN SQUARE ERROR ALGORITHM: Because of the nearness of guard insertion it is expected that there is no ISI. Presently got signal signified as Y, and it is communicated as:

$$\begin{aligned} Y &= XFH + W \quad X = \text{diag}\{X(0), X(1), \dots, X(N-1)\} \quad H = \text{diag}\{H(0), H(1), \dots, H(N-1)\} = \text{DFT}_N(h) \\ Y &= \text{diag}\{Y(0), Y(1), \dots, Y(N-1)\}^T \quad W = \text{diag}\{W(0), W(1), \dots, W(N-1)\}^T \end{aligned}$$

$$F = \begin{bmatrix} W_N^{00} & \cdot & \cdot & W_N^{0(N-1)} \\ \cdot & & & \cdot \\ \cdot & \cdot & & \cdot \\ \cdot & & & \cdot \\ W_N^{(N-1)0} & \cdot & \cdot & W_N^{(N-1)(N-1)} \end{bmatrix}$$

Where  $W_n^{nK} = \frac{1}{N} e^{-2j\pi(n/N)K}$

Now, the MMSE estimator can be defining as:

$$H_{MMSE} = FR_{hy} R^{-1}_{yy} Y$$

Where

$$R_{yy} = E\{hY\} = R_{hh} F^H X^H$$

$$R_{yy} = E\{YY\} = XFR_{hh} F^H X^H + \sigma^2 I_N$$

LESS COMPLEX MINIMUM MEAN SQUARE ERROR ALGORITHM USED FOR BETTER ESTIMATION:

As both the above calculations have some burdens. Like LS calculation has a weakness of high MSE then again MMSE calculation has some many-sided quality. So it requires new system which decreases both the issues [10]. As MMSE estimator characterized as

$$\hat{H}_{MMSE} = R_H (R_H + \sigma_n^2 (XX^H)^{-1})^{-1} \hat{H}_{LS}$$

Complexity with MMSE is reduced by putting  $(XX^H)^{-1}$  by expectation  $E(XX^H)^{-1}$

Now  $X = P \Lambda_x P^{-1}$

Where  $\Lambda_x$  is define the diagonal matrix & P is defined as Hermitian matrix.

Then  $(XX^H)^{-1}$  can be expressed as

$$\begin{aligned} (XX^H)^{-1} &= (P \Lambda_x P^{-1} \cdot (P \Lambda_x P^{-1})^H)^{-1} \\ &= [(P \Lambda_x)^{-1}]^H \cdot (P \Lambda_x)^{-1} \end{aligned}$$

Now, the MMSE equation become

$$H = R_H (R_H + \sigma_n^2 [(P \Lambda_x)^{-1}]^H \cdot (P \Lambda_x)^{-1})^{-1} \hat{H}_{LS} = R_H R_Y^{-1} \hat{H}_{LS}$$

$R_Y$  Can be describe by using SVD algorithm

$$\begin{aligned} R_y &= R_H + \sigma_n^2 [(P \Lambda_x)^{-1}]^H \cdot (P \Lambda_x)^{-1} \\ &= R_H + \sigma_n^2 U U^H \\ &= U \Lambda U^H \end{aligned}$$

Where  $U = [(P \Lambda_x)^{-1}]^H$  is unitary matrix and  $\Lambda = \text{diag}(\lambda_1, \lambda_2, \dots, \lambda_K)$

Now

$$\begin{aligned} \hat{H} &= (R_y - \sigma_n^2 U U^H) R_y^{-1} \hat{H}_{LS} \\ &= U (\Lambda - \sigma_n^2 I) U^H (U \Lambda U^H)^{-1} \hat{H}_{LS} \\ &= U \left( \frac{\Lambda - \sigma_n^2 I}{\Lambda} \right) U^H \hat{H}_{LS} \end{aligned}$$

#### IV. RESULT ANALYSIS

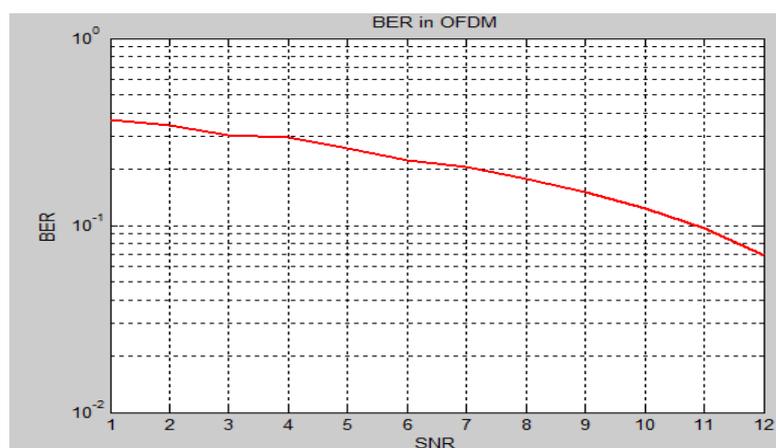


Figure 4.1 conventional OFDM with QPSK modulator

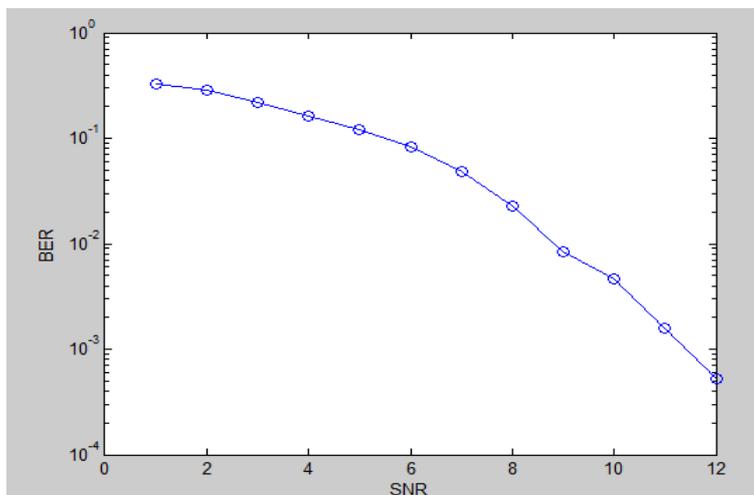


Figure 4.2 LS ESTIMATOR FOR QPSK MODULATION USING LINEAR INTERPOLATION

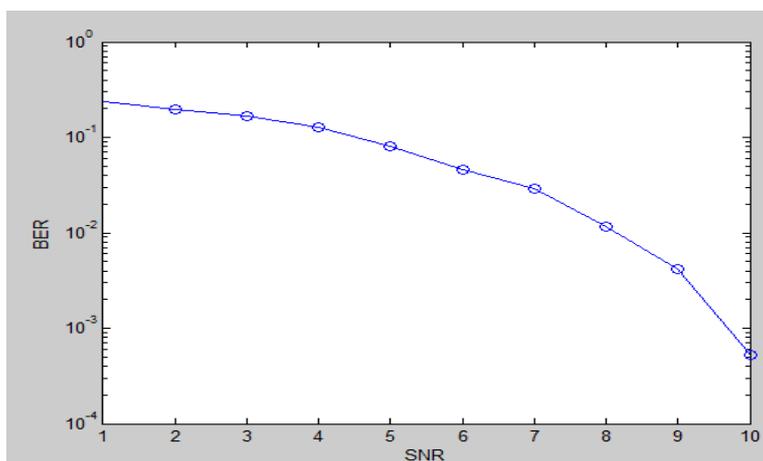


Figure 4.3 MMSE ESTIMATORS FOR OFDM USING QPSK MODULATION

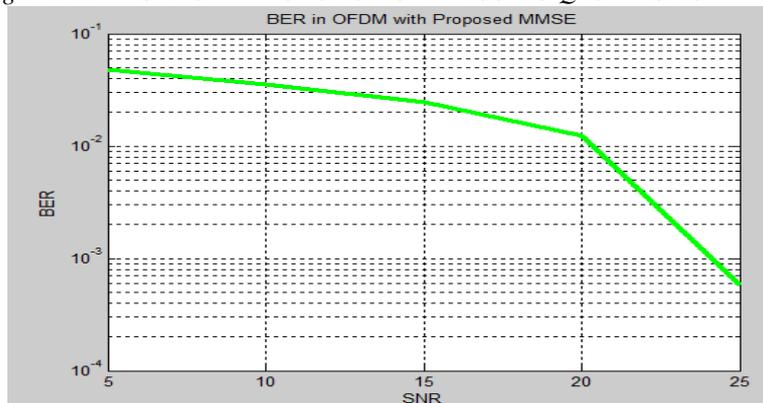


Figure 4.4 MODIFIED MMSE ESTIMATOR FOR OFDM USING QPSK MODULATION

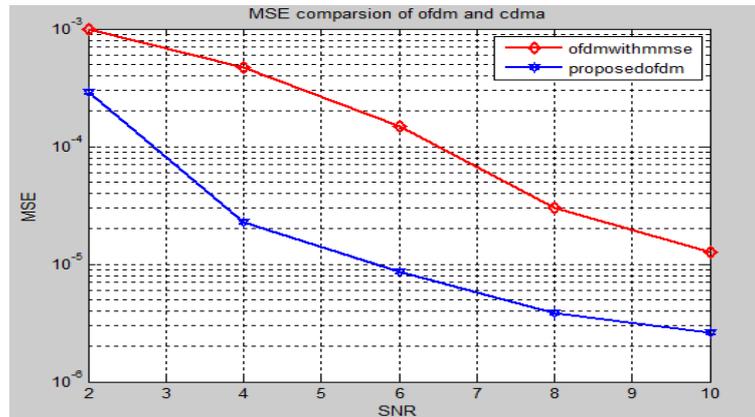


Figure 4.5 Comparison of performance in MMSE algorithm and Proposed MMSE in terms of SNR vs. MSE

## V. CONCLUSION

This paper contrasts the traditional OFDM and three channel estimation calculations and infers what strategy is ideal. In the wake of getting results the last conclusion is that both the LS calculation and MMSE calculation have experienced some impediments. As LS calculation comprise of high mean square error and MMSE calculation comprise of some multifaceted nature. In any case, in the wake of taking correlation between them two it is clear from the outcome that MMSE calculation gives preferred execution over LS calculation. MMSE calculations execution is better as far as mean square error. Be that as it may, unpredictability of MMSE calculation is enormous issue. So to decrease this many-sided quality less complex MMSE calculation is utilized. In the wake of breaking down the consequence of less complex MMSE, it is watch that less perplexing MMSE OFDM have preferable result over MMSE strategy, furthermore this system lessen level of many-sided quality.

## REFERENCES

- [1]. Srishtansh Pathak and Himanshu Sharma 'International Journal of Advanced Research in Computer Science and Software Engineering' Volume 3, Issue 3, March 2013.
- [2]. H. Meyr, M. Moeneclaey, and S. A. Fechtel, "Digital Communication Receivers", John Wiley and Sons, 1998.
- [3]. Shakuntala chouhan 'Channel Estimation Using LS and MMSE Estimators' Volume: 3 Issue: 8.
- [4]. M. Engels. Wireless OFDM Systems: Kluwer Academic Publishers, 2002.
- [5]. IEEE Standard 802.11a 1999. Wireless LAN Medium Access Control (MAC) and Physical Layer (PHY) Specifications: High-speed Physical Layer in the 5GHz Band. IEEE, September 1999.
- [6]. IEEE Standard 802.11b 1999. Wireless LAN Medium Access Control (MAC) and Physical Layer (PHY) Specifications: High-speed Physical Layer in the 2.4GHz Band. IEEE, September 1999.
- [7]. Gordan L. Stuber, "Principles of Mobile Communications", 2nd Edition, Kluwer Academic Publishers, 2 8.
- [8]. G. T. Zhou, M. Viberg, and T. McKelvey, "A first-order statistical method for channel estimation," IEEE Signal Processing Lett. vol. 10, no. 6, pp. 57-60, Mar. 2003.
- [9]. Y. Shen and E. Martinez, "Channel estimation in OFDM systems," Freescale Semiconductor, pp. 1-15, 2006.
- [10]. M. K. Ozdemir and H. Arslan, "Channel estimation for wireless OFDM systems," in IEEE Commun. Surveys Tutorials, vol. 9, no. 2, 2nd Quarter 2007, pp. 18-48.
- [11]. P. Hoeher, S. Kaiser, and P. Robertson, "Two-dimensional pilot-symbol-aided channel estimation by Wiener filtering," in Proc. ICASSP97, Munich, German, vol. 3, Apr. 1997, pp. 1845-1848.